## LOYOLA COLLEGE (AUTONOMOUS), CHENNAI - 600034

## B.Sc. DEGREE EXAMINATION - ECONOMICS

THIRD SEMESTER - NOVEMBER 2011

## ST 3103/3100 - RESOURCE MANAGEMENT TECHNIQUES

Date: 09-11-2011
Dept. No. $\square$ Max. : 100 Marks
Time : 9:00-12:00

## SECTION - A

Answer ALL questions. Each carries TWO marks.
(10 $\times 2=20$ marks $)$

1. In a General Linear Programming Problem, define the following terms:
(i) objective function
(ii) constraints.
2. Explain the following terms used in the general LPP:
(i) feasible solution
(ii) optimum solution.
3. Explain slack and surplus variables.
4. Formulate a Transportation Problem as a LPP.
5. Present the Transportation Table for an m-origin, $n$-destination Transportation Problem and write its rim requirements.
6. Define a LOOP in a transportation table.
7. Give an example of an assignment problem.
8. Explain the following terms used in sequencing:
(i) total elapsed time
(ii) No passing rule.
9. Explain the following terms used in a PERT network:
(i) optimistic time
(ii) pessimistic time
(iii) most likely time.
10. What are (i) set-up cost and (ii) ordering cost associated with inventories?
SECTION - B

Answer any FIVE questions. Each carries EIGHT marks.
11. A firm manufactures 3 products A, B, and C. The profit per unit sold of each product is Rs.3, Rs. 2, and Rs. 4 respectively. The time required to manufacture one unit of each of the three products and the daily capacity of the two machines P and Q is given in the table below:

| Machine | Time per unit (minutes)Product |  |  | Machine capacity (minutes / day) |
| :---: | :---: | :---: | :---: | :---: |
|  | A | B | C |  |
| P | 4 | 3 | 5 | 2,000 |
| Q | 2 | 2 | 4 | 2,500 |

It is required to determine the daily number of units to be manufactured for each product, so as to maximize the profit. However at least 100 A's, 200 B 's, and 50 C's, but no more than 150 A's. Assume that all the units produced are consumed in the market. Formulate this problem as a LPP.
12. Solve the following LPP by graphical method:

Minimize $\mathrm{z}=2 \mathrm{x}_{1}+\mathrm{x}_{2}$
subject to the constraints:

$$
\begin{aligned}
5 \mathrm{x}_{1}+10 \mathrm{x}_{2} & \leq 50 \\
\mathrm{x}_{1}+\mathrm{x}_{2} & \geq 1 \\
\mathrm{x}_{2} & \leq 4 \\
\mathrm{x}_{1}, \mathrm{x}_{2} & \geq 0 .
\end{aligned}
$$

13. Find all the basic solutions to the system of linear equations :

$$
\begin{array}{r}
x_{1}+2 x_{2}+x_{3}=4 \\
2 x_{1}+x_{2}+5 x_{3}=5
\end{array}
$$

Are the solutions degenerate?
14. Use simplex method to solve the following LPP:

Maximize $\mathrm{z}=107 \mathrm{x}_{1}+\mathrm{x}_{2}+2 \mathrm{x}_{3}$
subject to the constraints:

$$
\begin{aligned}
14 x_{1}+x_{2}-6 x_{3}+3 x_{4} & =7 \\
16 x_{1}+\frac{1}{2} x_{2}-6 x_{3} & \leq 5 \\
3 x_{1}-x_{2}-x_{3} & \leq 0 \\
x_{1}, x_{2}, x_{3}, x_{4} & \geq 0 .
\end{aligned}
$$

15. Determine an initial feasible solution to the following transportation problem using the North-West Corner Rule:

| Origin | Destination |  |  |  | Available |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{D}_{1}$ | $\mathrm{D}_{2}$ | $\mathrm{D}_{3}$ | $\mathrm{D}_{4}$ |  |
| $\mathrm{O}_{1}$ | 6 | 4 | 1 | 5 | 14 |
| $\mathrm{O}_{2}$ | 8 | 9 | 2 | 7 | 16 |
| $\mathrm{O}_{3}$ | 4 | 3 | 6 | 2 | 5 |
| Requirement | 6 | 10 | 15 | 4 | 35 |

16. Consider the problem of assigning five jobs to five persons. The assignment costs are given as follows:

| Persons | Job |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 2 | 3 | 4 | 5 |
| A | 8 | 4 | 2 | 6 | 1 |
| B | 0 | 9 | 5 | 5 | 4 |
| C | 3 | 8 | 9 | 2 | 6 |
| D | 4 | 3 | 1 | 0 | 3 |
| E | 9 | 5 | 8 | 9 | 5 |

Determine the optimum assignment schedule.
17. In a factory, there are six jobs to perform, each of which should go through two machines A and B , in the order $\mathrm{A}, \mathrm{B}$. The processing timings (in hours) for the jobs are given here. Determine the sequence for performing the jobs that would minimize the total elapsed time, T. What is the value of T ?

| Job $:$ | $\mathrm{J}_{1}$ | $\mathrm{~J}_{2}$ | $\mathrm{~J}_{3}$ | $\mathrm{~J}_{4}$ | $\mathrm{~J}_{5}$ | $\mathrm{~J}_{6}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Machine A : | 1 | 3 | 8 | 5 | 6 | 3 |
| Machine B : | 5 | 6 | 3 | 2 | 2 | 10 |

18. A project consists of seven activities for which relevant data are given below:

| Activity | Preceding Activities | Activity Duration (Days) |
| :---: | :---: | :---: |
| A | -- | 4 |
| B | -- | 7 |
| C | -- | 6 |
| D | A, B | 5 |
| E B B | 7 |  |
| F | C, D, E | 6 |
| G | C, D, E | 5 |

Draw the network and find the project completion time.
SECTION - C

Answer any TWO questions. Each carries TWENTY marks.
19(a) Solve graphically the following LPP:
Maximize $\mathrm{z}=10 \mathrm{x}_{2}-2 \mathrm{x}_{1}$
subject to the constraints:

$$
\begin{align*}
x_{1}-x_{2} & \geq 0 \\
-x_{1}+5 x_{2} & \geq 5 \\
x_{1}, x_{2} & \geq 0 . \tag{10}
\end{align*}
$$

(b) Write the characteristics of the standard form of LPP.

20(a) Obtain initial basic feasible solution of the following transportation problem using Vogel's method.

| Origin | Destination |  |  | Supply |
| :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{D}_{1}$ | $\mathrm{D}_{2}$ | $\mathrm{D}_{3}$ |  |
| $\mathrm{O}_{1}$ | 13 | 15 | 16 | 17 |
| $\mathrm{O}_{2}$ | 7 | 11 | 2 | 12 |
| $\mathrm{O}_{3}$ | 19 | 20 | 9 | 16 |
| Demand | 14 | 8 | 23 |  |

(b) Explain the concept of EOQ and draw the graph of EOQ.
21. Determine the optimal sequence of jobs that minimizes the total elapsed time based on the following information on processing time on machines given in hours and passing is not allowed:

| Job $:$ | A | B | C | D | E | F | G |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Machine $\mathrm{M}_{1}:$ | 3 | 8 | 7 | 4 | 9 | 8 | 7 |
| Machine $\mathrm{M}_{2}:$ | 4 | 3 | 2 | 5 | 1 | 4 | 3 |
| Machine $\mathrm{M}_{3}:$ | 6 | 7 | 5 | 11 | 5 | 6 | 12 |

[^0]22. A project consists of eight activities with the following relevant information:

| Activity | Immediate Predecessor | Estimated duration (days) |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | Optimistic | Most likely | Pessimistic |
| A | -- | 1 | 1 | 7 |
| B | -- | 1 | 4 | 7 |
| C | -- | 2 | 2 | 8 |
| D | A | 1 | 1 | 1 |
| E | B | 2 | 5 | 14 |
| F | C | 2 | 5 | 8 |
| G | D, E | 3 | 6 | 15 |
| H | F, G | 1 | 2 | 3 |

(i) Draw the PERT network and find out the expected project completion time.
(ii) What duration will have $95 \%$ confidence for project completion?


[^0]:    Find the minimum total elapsed time and the idle time of the machines.

